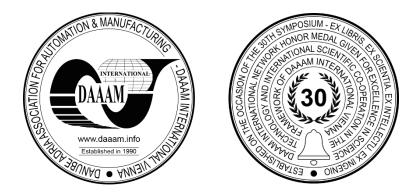
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MACHINE LEARNING FOR DATA ANALYSIS IN FOOTBALL: A SURVEY OF METHODS AND PROBLEMS

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Abstract

Machine learning is growing exponentially, and its applications are gaining more traction in the sports analysis community in recent years. The application of machine learning methods on spatiotemporal data in sports like football is getting attention from football clubs, academics, and amateur analysts and is the focus of this survey. This survey analyses and identifies current trends in research papers and literature to determine current and future applications in football analytics using spatiotemporal data.

Keywords: spatiotemporal data; sports analytics, event data; deep neural networks, machine learning

1. Introduction

Sports analytics in sports clubs has been evolving ever since "Moneyball" [1] showed how applied statistics could be used to select less know but valuable baseball players. While many sports, including football, have had rich data for decades until recently, spatiotemporal data was unavailable, and the advancement of technical capabilities enabled the evolution of available data. While so-called match sheet data certainly has its' value and is mainly understood by experts and laymen alike, spatiotemporal data opens new possibilities for clubs and scouts. Unfortunately, football clubs focus primarily on video analysis, which is highly time-consuming and introduces bias. Spatiotemporal event data helps in answering many practical questions of much interest in football clubs like:

- Calculate the probability of scoring a goal from a given situation?
- How to evaluate a particular pass?
- What are common tactics opponents use?
- Which players have similar playing styles?

This paper analyses and identifies current trends in research papers and literature to determine current and future applications in sports analytics using machine learning and spatiotemporal data. The goal of this research was to research the current state of data types, data availability, and research methods and applications of machine learning in sports analytics, focusing on applied research in football. Before the literature overview was conducted, we proposed the following research questions:

33RD DAAAM INTERNATIONAL SYMPOSIUM ON INTELLIGENT MANUFACTURING AND AUTOMATION

- Research question 1: How to categorize current research in machine learning in football analytics
- Research question 2: What are common methods of machine learning in football analytics
- Research question 3: What are possible further research directions

To answer our research questions, we've conducted a comprehensive literature overview using the Systematic Literature Review approach [2] to gather recent literature. The main goal was to classify recent research and analyse then categorize it by applying the content analysis method. The result of the analysis showed that the literature could be classified broadly as applying machine learning to spatiotemporal data in football to:

- Evaluate individual players
- Evaluate passes/actions
- Evaluate and classify teams
- Game result prediction

This paper is organized as follows: first, we introduce the domain of sports analytics and systemize the types of data and their availability; second, we provide an overview of recent research in the field of machine learning and spatiotemporal data in football; finally, we give a conclusion of the current state and suggest further research directions possible.

2. Data types and availability

Data suitable for football (soccer in the USA) analytics can be divided into three categories:

- Match sheet data
- Event data
- Tracking data

All types of data are obtained from specialized companies or websites. For example, service providers like FBref [3] usually provide match sheet data without fees, while event and tracking data are only available under a proprietary license. Some existing open datasets of event data are provided by providers like Wyscout [4] and Statsbomb [5]. Tracking data providers include Opta [6], Signality [7], SecondSpectrum [8], Metrica [9], and others.

Match sheet data provides a high-level statistic of the game, player, or club. In general, this data is freely accessible, and some websites even encourage the public to "scrape" the data from them. Many sources like FBref [3] provide additional statistical data, such as adding Expected Goals and Expected Assists. Still, this kind of data doesn't help answer complex questions club stakeholders might have. Event data is a sparser type of data, like tracking data; it is generated from video by human annotators and consists of current player and ball positions. Data points occur after a particular event like a pass, goal, foul or other.

Although this data also is usually not freely available, some available datasets are appropriate for research. The most significant difference between event and tracking data is that tracking data tracks the position of all players on the pitch. In contrast, event data only records the event, disregarding other players' positions. Pappalardo describes the biggest available dataset to date in [10]. Data covers the seven most significant European leagues, World Cup 2018. and European cup 2016. Event data consists of events like pass, foul, and others with subtypes like cross-pass.

Tracking (spatiotemporal) data represents a type of data that consists of both time and space with unique properties regarding the modeling of spatio-temporal relations [11]. For example, in sports, there are usually 10-30 data points per second (10-30Hz) representing players' current positions on the pitch plus the ball. Tracking data can be obtained in multiple ways – static cameras, commercial video broadcasts, and GPS devices. However, due to its high commercial value, it is challenging for researchers to obtain this data type. Therefore, this data type is usually reserved for analysts in clubs with access to their league data. Khaustov and Mozgovoy [12] propose "a rule-based algorithm for identifying several basic types of events in soccer, including ball possession, successful and unsuccessful passes, and shots on goal." Direct potential benefits of applying their algorithm to tracking data could enhance additional event information usually unavailable as part of tracking data., p.

3. Research

The research questions in the introduction are self-evident, bearing in mind that the research is broadly interested in the state-of-art machine learning applications in spatiotemporal data analysis in football. Systematic Literature Review guidelines [2] are used to answer these questions. In that sense, a literature search was conducted extensively in the IEEE Xplore Digital Library (IEEE), Scopus database, Web of Science database (WoS), ScienceDirect, and Google Scholar. Furthermore, due to the specificity of the research topic, search terms include a specific combination of targeted keywords, e.g., "Machine learning" AND "spatiotemporal" AND "football" OR "soccer" and many others. In the next step, we created a table where we classified all the research papers by data type used (event or tracking), machine learning method, practical application, and broad categories that could group relevant papers. Some research papers were included in more than one category.

33RD DAAAM INTERNATIONAL SYMPOSIUM ON INTELLIGENT MANUFACTURING AND AUTOMATION

The research categories that were most apparent from the literature overview of 45 most recent or most important research papers with a corresponding number of papers are as follows:

- Evaluate individual players (13)
- Evaluate passes/actions (12)
- Evaluate and classify teams (11)
- Game result prediction (8)

4. Results

After the literature overview it became evident that the application of machine learning models to football analysis varies from so-called classical methods like a k-nearest neighbours to complex neural networks. One of the most compelling papers which provide football-applicable CNN architecture [13] is "Soccermap" [14] shown in Figure 1

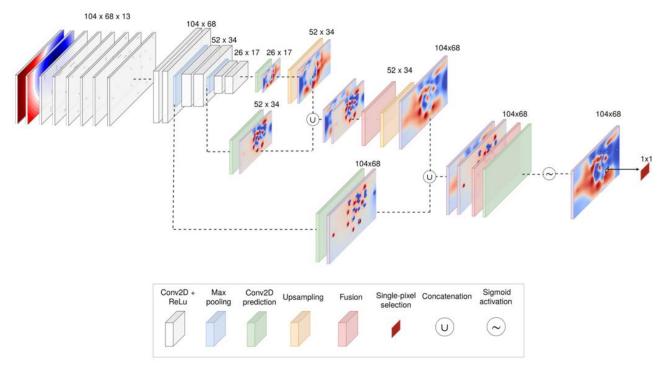


Fig. 1. Soccermap CNN, [14]

This architecture demonstrates that it is possible to apply modern machine learning approaches to tracking data with practical applications in football. By changing only, the output function, this network can calculate the probability surfaces of potential passes, estimate the pass-selection likelihood, and predict the expected value of the pass. In Table 1, we've organized the most recent and influential research in machine learning in football, mainly focusing on spatiotemporal data. Correspondingly, we provide an overview of data types, methods, practical applications, and identified tasks.

Reference	Data	Method	Application	Task
Cintia et al. [15]	Event	k-means, autoencoder	capturing and analysing the playing style of players, teams, and coaches in an automatic way	Evaluate and classify teams
Fernández et al. [16]	Tracking	Markov decision process	ability to evaluate the impact of observed and potential actions, both visually and analytically, expected possession value	Evaluate passes/actions
Hyeonah et al. [17]	Event	Convolutional Autoencoder	characterizing player's styles	Evaluate passes/actions
Kim et al [18]	Tracking	CNN, embeddings	Detecting players and their styles	Evaluate individual players
Lee and Jung [19]	Match sheet	DNN	predicting soccer tactics	Evaluate and classify teams
Malamatinos et al. [20]	Match sheet	k-Nearest Neighbour (k-NN), LogitBoost (LB), Support Vector Machine (SVM), Random Forest (RF), and CatBoost (CB)		Game result prediction

$33 \mbox{rd}$ DAAAM International Symposium on Intelligent Manufacturing and Automation

Kim et al. [21]	Tracking	graph based CPD	distinguishes tactically intended formation and role changes from temporary changes in soccer	Evaluate and classify teams
Clijmans et al. [22]	Event	Markov model	matches analysing playing style	Evaluate and classify
Goes et al. [23]	Tracking	KMeans	Classify attacks as successful	teams Evaluate passes/action
Fernàndez et al. [14]	Tracking	CNN	probability surfaces of potential passes, the expected value of a pass	Evaluate passes/action
Goes et al. [24]	Tracking	KMeans	defenders create space for attackers are strongly dependent on those attacks' success	Evaluate passes/action
Raabe et al. [25]	Event	Graph neural networks	Analysing tactical patterns	Evaluate and classify teams
Verstraete et al. [26]		CPD (canonical polyadic decomposition) [27]		Evaluate individual players
Nunez and Dagnino [28]		pitch control, expected possession value and expected goals in a weighted function	Google Research Football competition [29]	-
Liu et al. [30]	Event	Deep Reinforcement Learning, LSTM	developed a new metric called GIM, to evaluate teams	Evaluate and classify teams
Decroos et al.[31]	Event	non-negative matrix factorization [32]	identifying players with a similar style	Evaluate individual players
Beal et al. [33]	Event	walks within graphs, mixed integer programming	forming teams with	Evaluate individual players
Pappalardo et al. [34]	Event	Linear Support Vector Classifier	role-aware player performance evaluation	Evaluate individual players
Groll et al. [35]	Event	random forests and Poisson ranking		Game result prediction
Goes et al. [36]	Tracking	Principal component analysis [37]	evaluating pass value	Evaluate passes/action
Dick et al. [38]	Tracking	deep reinforcement learning	valuations of multiple players positioning	Evaluate individual players
Yam [39]	Tracking	deep reinforcement learning	valuations of multiple players positioning	Evaluate individual players
Decroos et al. [40]	Event	Generalized Additive Model [41] distance-weighted k-nearest	improvement to VAEP model [42]	Evaluate passes/action
Bransen et al. [43]	Event	neighbours search	a new metric that aims to measure players' contribution in creating goal-scoring chances	Evaluate individual players
Zambom-Ferraresi et al. [44]	Tracking	Bayesian model averaging [45]	discover determinants of sports performance	Evaluate passes/action
Steiner et al. [46]	Tracking	binary logistic regressions	estimate the effects of contextual features on passing decisions	Evaluate passes/action
Pappalardo et al. [47]	Tracking	OLS regression and logit classification	finds team ranking in the future season by using data from previous seasons	Evaluate and classify teams
McHale et al. [48]	Tracking	probability of a successful pass and network centrality measures	help trainers and scouts identify vital players in either opposition teams when recruiting new talents	Evaluate individual players
Giancola et al. [49]	-	CNN, ResNet-152	detecting events in football broadcast videos	-
Decroos 20/12/2022 23:23:00et al. [49]	Event	clustering	discover tactics of football teams	Evaluate and classify teams
Decroos et al. [42]	Event	Clustering, exponential- decay-based	find top performing players in a league or a particular match	Evaluate individual players
Steiner 20/12/2022 23:23:00et al. [46]	Event	regression model	whom the player is most likely to pass the ball	Evaluate passes/action
Horton et al. [50]	Tracking	computational geometry features fed into different classifiers (MLR, SVM, RUSBoost	classify the quality of passes in football	Evaluate passes/action
Brooks et al. [51]	Event	L2-regularized Support Vector Machine (SVM) model	rank players based on the value of their passes	Evaluate individual players / Evaluate passes/actions
Brooks et al. [52]	Event	KNN	create a unique team identification	Evaluate and classify teams

33rd DAAAM INTERNATIONAL SYMPOSIUM ON INTELLIGENT MANUFACTURING AND AUTOMATION

McHale et al. [53]	Event	mixed-effects model	model for identifying the ability of football players to score goals	Evaluate individual players
Bialkowski et al. [54]	Tracking	minimum entropy data partitioning and expectation- maximization (EM) algorithm	analysing both individual players and teams	Evaluate and classify teams / Evaluate individual players
Bialkowski et al. [55]	Tracking	LDA/ k-NN	identifying teams from spatiotemporal tracking data	Evaluate and classify teams
Tewari et al. [56]		XGboost, SVM, Logistic regression	-	Game result prediction
Baboota et al. [57]		Gaussian naive Bayes, SVM, Random forest, and gradient boosting		Game result prediction
Razali et al. [58]		Bayesian networks		Game result prediction
Danisik et al. [59]		LSTM regression model		Game result prediction
Cho et al. [60]		gradient boosting		Game result prediction
Ulmer et al. [61]		Naive Bayes, Hidden Markov Model, Multinomial Naive Bayes, RBF SVM, Random forest, Linear SVM, One vs. All SGD		Game result prediction

Table 1. Literature overview, Source: authors contribution

5. Conclusion

This review aimed to evaluate the current state of machine learning in sports analytics, particularly interested in applications on data analytics in football. While the field might seem like a niche category, the number of research papers and non-academic content was pretty significant, so we've decided to focus on the most recent studies most representative of the current state-of-the-affairs. Besides many possible research directions from the literature, this review detects four main research tasks. These tasks are:

- players evaluation
- passes and actions evaluation
- team evaluation
- game result prediction

It is no surprise that most tasks have practical applications that are of interest to football club stakeholders. Such claims include scouting, which stems from player evaluation, overall team formation improvement by combining player evaluation and team evaluation, and team success expectations by combining all four tasks are just a few of many. The coaching staff has many benefits, including tactical preparations of matches from passes/actions evaluation, players evaluation, and opposing team evaluation. In addition, game result predictions are also of interest to sports betting as in academic research.

On the other hand, conducted results show that methods in this area span from so-called classical machine learning to deep learning, which has been the dominant method in recent times. Also, data types are closely related to the method used; in that sense, CNN models have shown the most promising research direction. We intentionally omit the area of simulation environments methods from this survey because it is the emerging approach to addressing problems. Among them, we would like to point out possible research directions in simulated multi-agent environments like Google Research Football as a method for coping with defined tasks.

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