THERMAL SIMULATIONS BASED ON MACRO-MODELS

Václav Marek, Zdeněk Hájiček

Abstract

Thermal transfer simulations, computed fluid dynamic solutions and finite element methods in general are vital sources of information about behavior of machine parts with heat loading. All these methods have common disadvantages, which include the requirements of a skilled engineer, hardware and software, and generally the high cost of computation. These problems are solved in this article. The reduction of costs is solved by a new tool, which uses simple macro-elements with predefined, parametric properties. These elements are able to describe cooling channels, heat transfers in bodies or identify the temperatures of heat sources. Computation by macro-element method takes a significantly shorter time with suitable accuracy. The macro-element method is suitable for customizing in a wide spectrum of thermal transfer cases. The article defines macro-elements, describes their implementation and the verification of the method.

Keywords: thermal simulation; liquid-cooled spindle unit; macro-element method, thermal displacements

1. Introduction

Machine tools are highly sophisticated mechatronic systems enabling manufacturing processes at a given precision. A machine tool’s precision strongly depends on its thermo-elastic behaviour [8]: Internal and external heat sources lead to a non-uniform and non-nominal temperature distribution resulting in elongation and mechanical deformations of the machine tool structure. One of the main factors in mastering the thermal behavior of machine tools is effective cooling. It can be achieved by conduction through solid parts, by radiation, by free or enforced convection on outer surfaces or by forced convection with liquid cooling systems. The non-uniform distribution leads to areas with higher thermal load, such as the main drive, the bearings or the cutting tool. Direct cooling of cutting tools is used in almost every cutting process. It provides cooling of the tool and lubricates the cutting area. In order to reduce thermally induced displacements, fluid based cooling systems are used. Main drives of machines can be cooled by air or by liquid circuits, while bearings are often cooled by liquid circuits and oil mist. Thus, controlling the thermo-elastic behavior of machine tools is to a large extent depending on the design of their fluidic system. In order to speed up the development and minimize the necessity of physical prototypes, it is essential to verify the design before manufacturing. Simulation of a complex system is laborious task: It requires time to prepare computer aided design (CAD) models, skilled employees and computation time.

This paper follows up an idea of macro-models. Weber describes the approach for a heat-loaded motorized spindle unit [5]. It uses a network based computation model. It describes the transient, three-dimensional energy exchange processes in built-in motorized spindles – especially in a cooling sleeve with a single helical rectangular water-cooling
channel. [1] A similar approach is used by Institute of Machine Tools and Manufacturing (IWF), at ETH Zurich (the Swiss Federal Institute of Technology in Zurich). It is characterized by the description of a cooling channel as a series of predefined, but parametric geometric features. The tool predicts the heat transfer properties and pressure loss to be expected for a given operational point and coolant. According to the authors, the main advantage is the simplicity of use, and significantly shorter computation times than with a CFD approach [8].

1.1 Current state

The macro-element method is based on simple elements. Macro-elements are distinct elements, defined by elementary equations. The method produces a description of the properties of a fluid in one dimensional dependency. The properties of the macro-element depend on the properties of the fluid, the duct geometry and the operational point [1, 2]. The properties of a wall like roughness also influence the results [9]. These dependencies determine pressure losses and heat transfer coefficients which are the two significant factors in cooling circuits. Macro-elements can be identified in Figure 1, which shows a CFD simulation of a cooling circuit. It is a solved case of CFD simulation. The simulation consists of 2x10^5 elements, takes about 7 minutes and the solver uses a K-epsilon turbulent model of computation. This case is solved in NX10 simulation software. Examples of identified macro-elements are shown in table 1.

![CFD simulation of pressure losses in cooling circuit (NX10)](image)

**Fig. 1. CFD simulation of pressure losses in cooling circuit (NX10)**

<table>
<thead>
<tr>
<th>Channel</th>
<th>cooling channel, rectangular/circular</th>
</tr>
</thead>
<tbody>
<tr>
<td>Elbow</td>
<td>elbow element, rectangular/circular</td>
</tr>
<tr>
<td>Helix channel</td>
<td>helix-shape cooling channel</td>
</tr>
<tr>
<td>Flow-Around</td>
<td>element used for cooling of a bearings</td>
</tr>
<tr>
<td>Fitting</td>
<td>connection, section change</td>
</tr>
</tbody>
</table>

Table 1. Basic macro-elements

2. Pressure loss

Macro-element definition consists of this pressure loss computation. Pressure loss is an important property of each macro-element. It is a necessary parameter for identifying the overall pressure loss in the cooling channel. The pressure loss $\Delta p$ depends on velocity $w$, density $\rho$ and friction coefficient $\zeta_u$.

$$\Delta p = \frac{\zeta_u \rho w^2}{2} [Pa]$$  (1)

According to [4].
The friction coefficient is computed empirically:

$$\zeta_u = f(Re, D, r)$$  (2)
with the Reynolds number

\[ Re = \frac{wD}{\nu} \]  

and the pipe hydraulic diameter \( D \) of the pipe, the kinematic viscosity \( \nu \).

3. Verification of pressure losses

Calculations of properties are executed in order to define the basic shapes of each macro-element. The theoretical properties of the macro-elements presented in [2] were stated by using the equation for laminar and turbulent flow as presented in [7]. To verify the results of this theoretical equation, two commercially available CFD simulation software solutions are used: Ansys and Siemens NX. For each macro-element simulation, various operational and geometric conditions are considered [10]. These simulations provide the pressure loss and heat transfer coefficient (htc). Using these results in combination with the results of the macro-models, the macro-elements are verified. The result of CFD simulation of a macro-element can be seen in Figure 2. Verification was generally proved with flow 1x10^{-3}[m^3/s] with parametric variable dimensions. The graph in Figure 3 shows a comparison of CFD and macro-model computation. As can be seen, the results are very similar. The results of a specific case are shown in Table 1.

![CFD simulation of total pressure in flow in rectangular elbow](image1.png)

![Comparison of macro-element computation and CFD simulation](image2.png)

### Table 2. Results of computation of elbow with rectangular section

<table>
<thead>
<tr>
<th>solver</th>
<th>section</th>
<th>dim.a [mm]</th>
<th>dim.b [mm]</th>
<th>Radius [mm]</th>
<th>Flow [m^3/s]</th>
<th>Pressure loss [Pa]</th>
</tr>
</thead>
<tbody>
<tr>
<td>NX10</td>
<td>Rectang.</td>
<td>10</td>
<td>20</td>
<td>25</td>
<td>1x10^{-3}</td>
<td>2874</td>
</tr>
<tr>
<td>DD</td>
<td>Rectang.</td>
<td>10</td>
<td>20</td>
<td>25</td>
<td>1x10^{-3}</td>
<td>2245</td>
</tr>
<tr>
<td>ANSYS</td>
<td>Rectang.</td>
<td>10</td>
<td>20</td>
<td>25</td>
<td>1x10^{-3}</td>
<td>2950</td>
</tr>
</tbody>
</table>
4. Thermal field computation

The cooling characteristic is defined by thermal field computation. A similar approach as for pressure loss is performed. The element which performs heat transfer is examined. Heat transfer by convection is governed by the value of the heat transfer coefficient $u$ or $h$ [W/m$^2$K]. The value of $h$ depends on different quantities, including distinct physical characteristics of the fluid in question. Those are the isobaric specific heat (in J/kg K), the thermal conductivity (in W/m K) and the dynamic viscosity (in kg/ms) [6,7]:

$$h_{convec} = Nu D \frac{1}{\delta}$$  \hspace{1cm} (4)

$$Nu D = Nu D(Re_D, Pr)$$  \hspace{1cm} (5)

$h_{convec}$ – heat transfer coefficient for heat convection in cooling channel  
$Nu$ – Nusselt’s number  
$Pr$ – Prandtl’s number  
$D$ – hydraulic diameter  
$\lambda$ - heat conductivity

4.1. Thermal phenomena in a motorized spindle

A spindle of a milling machine was chosen as an example of thermal phenomena. The motorized unit of a spindle of a milling machine consist of a few main parts which affect the thermal behavior of this assembly. [7]

- heat sources in the stator  
- heat sources in the rotor  
- heat sources and friction in bearing  
- heat sources and friction in air gaps  
- heat transfer between shaft and rotor  
- heat transfer between housing and coolant

These effects are investigated.

4.2. Temperature field

Given an element with a constant wall temperature as boundary condition, the temperature at position $x$ and the wall heat flux can be calculated using the solution of the corresponding partial differential equation (PDE):

$$T(x) = T_w + \exp \left( - \frac{U \cdot R_{th}}{c_p \cdot m} \right) \cdot (T_{in} - T_w)$$  \hspace{1cm} (6)

$$Q_w = (T(L) - T_{in}) \cdot c_p \cdot m$$  \hspace{1cm} (7)

$T_w$ – Wall temperature  
$T_{in}$ – Inlet temperature (outlet temp. of the prev. element)  
$Q_w$ – Wall heat flux  
$U$ – Profile circumferential length  
$R_{th}$ - Thermal resistance between the wall and the fluid  
$c_p$ – Specific heat capacity of the fluid  
$m$ – Mass flow rate through the element  
$L$ – Element length

The conductive thermal resistance $R_w$ of the wall and the surface $A$ and $h_{convec}$ on the inside of the element:

$$R_{th} = \left( \frac{1}{R_w} + \frac{1}{\alpha A} \right)^{-1}$$  \hspace{1cm} (8)

4.3. Thermal resistance of a wall

Thermal resistance is calculated as:

$$R_w = A \cdot \frac{1}{\delta}$$  \hspace{1cm} (9)
δ – Thickness of the wall
λ – Thermal conductivity of the wall
A – Surface of the wall

For a cylindrical element, the thermal resistance of the wall is calculated as follows [3]:

\[ R_w = \frac{2 \cdot \pi \cdot L \cdot \lambda}{\ln\left(\frac{r_o}{r_i}\right)} \] (10)

\( r_o \) – Outside radius of the element
\( r_i \) – Inside radius of the element

5. Verification of thermal-field computation

Figure 4 shows the results of a CFD simulation of a macro-model. The CFD simulation in the picture shows temperatures in the housing and temperatures of the cooling fluid. In this comparison, the flow around the model was tested. The bearing unit simulation consists of a heat source which substitutes heat loss of bearing, in this case 800[W]. Cooling is provided by water with a flow of 0.4[kg/s].

The macro-model of the flow-around computes the heat transfer with good precision as can be seen in Figure 6. The temperature of output water is almost identical as computed by CFD, shown in Figure 5. Also, other computed temperatures of the wall and bearings are similar, given in Figure 6. The macro-model computation provides the correct information dependent on parametric dimensions, flow of coolant etc.

![Fig. 4. CFD simulation (NX10) of temperatures of cooled bearing housing](image)

![Fig. 5. Comparison of CFD and macro-element simulation - temperatures of outlet water](image)
6. New tool

The interface for the macro-element method computation is a tool called DuctDesigner. This tool was developed by the Institute of Machine Tools and Manufacturing (IWF), at ETH Zurich (the Swiss Federal Institute of Technology in Zurich). A Comparative calculation of the same cooling circuit performed by using the macro-element method provides results almost immediately. Results are shown in the graph in Figure 7. The simulation of a complex cooling circuit of a motorized spindle unit was performed. Figure 7 shows the results from a CFD simulation of the cooling circuit. Macro-element computation is shown in Figure 7. It shows pressure losses, temperatures and the heat transfer coefficient along the path of the cooling circuit. Pressure decrease can be seen in the graph, with an overall pressure loss of $3 \times 10^5$ [Pa]. It also shows the results of temperature computation and heat transfer coefficient computation. Temperature results are given in Table 3.
7. Discussion

Temperature field computed by macro-elements is pretty same as CFD simulation. Temperature obtained by macro-elements is a function driven by a few input parameters (flow, fluid properties, channel dimensions etc.). It causes faster computation then CFD, which operates with many parameters of every single finite element.

Macro-element computation does not provide detail results, because of these facts. It provides required information, corresponding the design process. Comparison of method is shown in the Table 4. The table shows main differences between CFD calculation and macro-element prediction.

<table>
<thead>
<tr>
<th></th>
<th>Prepare time</th>
<th>Comp. time</th>
<th>Temp. Comp.</th>
<th>Result deviation</th>
<th>Costs</th>
</tr>
</thead>
<tbody>
<tr>
<td>CFD</td>
<td>1hour</td>
<td>&gt;600s</td>
<td>full</td>
<td>&lt;5%</td>
<td>High</td>
</tr>
<tr>
<td>Macro-model</td>
<td>1/2hour</td>
<td>&lt;1s</td>
<td>partial</td>
<td>&lt;20%</td>
<td>Low</td>
</tr>
</tbody>
</table>

Table 4. Comparison of CFD and macro-element method

8. Conclusion

Overview of a design of a heat loaded machine was done in this paper. Macro-element method was integrated into a design and simulation process. Principles of the decomposition of a complex case to elementary case was described. The usability of the improved DuctDesigner software is demonstrated.

Its Macro-element calculation provides less calculation cost, shorter time configuration and no high skill requirements of users, as can be seen in Table 4. At this point, the concept of macro-elements is not a substitute of CFD or FEM, but it is an important addition to the existing design process. Similar results of CFD calculation and macro-element calculation verify precision of element computation. Results of this research should be verified by experiments. Experiments are included in plan.

9. Outlook

A systematic verification of the existing macro models is thus required, to improve the performance of these models. Experimental measurement of single macro-elements and complex systems simulated by macro-elements is also required for verification. The main potential is identified in the possibility of using the method in a wide range of applications, in the prediction of parameters of a flow, thermal transfer effects and cases of heat loaded machine parts. Obtained data will be used for a research focused on compensation of thermal displacements of milling centres. Macro-element methodology will be optimize for prediction of thermal field in the spindles of large milling machines.

10. Acknowledgement

The project LO1502 'Development of the Regional Technological Institute' is carried out under the auspices of the National Sustainability Program I of the Ministry of Education of the Czech Republic
11. References


